

Пример 14

$$\sin 4x - \cos 2x = 0$$

$$2\sin 2x \cos 2x - \cos 2x = 0$$

$$\cos 2x (2\sin 2x - 1) = 0$$

$$\begin{cases} \cos 2x = 0, \\ 2\sin 2x - 1 = 0; \end{cases} \Leftrightarrow \begin{cases} \cos 2x = 0, \\ \sin 2x = \frac{1}{2}; \end{cases} \Leftrightarrow$$

$$\begin{cases} 2x = \frac{\pi}{2} + \pi n, n \in \mathbb{Z} \\ 2x = (-1)^k \arcsin \frac{1}{2} + \pi k, k \in \mathbb{Z} \end{cases} \Leftrightarrow \begin{cases} x = \frac{\pi}{4} + \frac{\pi n}{2}, n \in \mathbb{Z} \\ x = (-1)^k \frac{\pi}{12} + \frac{\pi k}{2}, k \in \mathbb{Z} \end{cases}$$

$$\text{Ответ : } \frac{\pi}{4} + \frac{\pi n}{2}, n \in \mathbb{Z}; \quad (-1)^k \frac{\pi}{12} + \frac{\pi k}{2}, k \in \mathbb{Z}.$$