

# Compressed Sensing – basic idea

- A signal, which is **sparse** in some representation, can be undersampled (skip measurements) and then reconstructed mathematically
- Full sampling:  $Fx = y$  (full system),  
 $F$  – inverse Fourier transform,  $x$  – spectrum,  $y$  – FID  
Undersampling:  $\tilde{F}x = \tilde{y}$  (undetermined system)  
CS reconstruction:  $\min_x \|x\|_p$  subject to  $\tilde{F}x = \tilde{y}$   
(out of all possible FIDs choose the one which gives the sparsest spectrum)

Taking noise into account:  $\min_x \left( \|\tilde{F}x - \tilde{y}\|_2 + \lambda \|x\|_p \right)$